

GW190521: A Binary Black Hole Merger with a Total Mass of $150M_{\odot}$

The LIGO Scientific Collaboration and the Virgo Collaboration
(compiled May 30, 2020)

On May 21, 2019 at 03:02:29 UTC Advanced LIGO and Advanced Virgo observed a short duration gravitational-wave signal, GW190521, with a three-detector network signal-to-noise ratio of 14.7, and an estimated false-alarm rate of 1 in 4900 yr using a search sensitive to generic transients. Assuming a quasicircular binary inspiral, GW190521 is consistent with the merger of two highly spinning black holes with masses of $85_{-14}^{+20}M_{\odot}$ and $65_{-17}^{+17}M_{\odot}$ (90% credible intervals). We infer that the primary black hole mass lies within the gap produced by (pulsational) pair-instability supernova processes, with only a 0.36% probability of being below $65M_{\odot}$. We calculate the mass of the remnant to be $142_{-16}^{+23}M_{\odot}$, which can be considered an intermediate mass black hole (IMBH). The luminosity distance of the source is $5.3_{-2.2}^{+2.2}$ Gpc, corresponding to a redshift of $0.82_{-0.29}^{+0.27}$. The inferred rate of mergers similar to GW190521 is $0.13_{-0.11}^{+0.30}$ Gpc $^{-3}$ yr $^{-1}$.

Introduction.— Advanced LIGO [1] and Advanced Virgo [2] have demonstrated a new means to observe the Universe through the detection of gravitational waves (GWs). In their first two observing runs (O1 and O2) the LIGO Scientific Collaboration and the Virgo Collaboration (LVC) have reported the detection of GWs from 10 binary black hole (BH) mergers, and a binary neutron star inspiral [3, 4]. The third observing run (O3) started on April 1, 2019, and was suspended on March 27, 2020; numerous public alerts pertaining to possible detections have been sent to the astronomical community [5], with two confirmed detections [6, 7].

The discovery of GW150914 [8] and subsequent events has revealed a population of binary BHs with total masses between $18.6M_{\odot}$ and $84.4M_{\odot}$, with component masses ranging from $7.6M_{\odot}$ to $50.2M_{\odot}$ [3]. A signal consistent with heavier BHs (170817+03:02:46UTC) has also been reported in [9, 10], albeit with a non-negligible chance of having an instrumental origin. For the parametrized population models considered in [11] it was inferred that no more than 1% of primary BH masses in merging binaries are greater than $45M_{\odot}$.

In this letter we expand this mass range with the confident detection of GW190521, a GW signal consistent with a binary BH merger of total mass $\sim 150M_{\odot}$, leaving behind a $\sim 140M_{\odot}$ remnant. Waveform models for quasicircular binary BHs indicate that a precessing orbital plane is slightly favored over a fixed plane. The observation of the ringdown signal from the remnant BH provides estimates for the final mass and spin that are consistent with those from the full waveform analysis.

It is predicted that stars with a helium core mass in the range of $\sim 32 - 64M_{\odot}$ are subject to pulsational pair instability, leaving behind remnants with mass less than $\sim 64M_{\odot}$. Stars with helium core mass in the range $\sim 64 - 135M_{\odot}$ would be susceptible to pair instability and leave no compact remnant, while stars with helium mass $\gtrsim 135M_{\odot}$ are thought to directly collapse to intermediate mass BHs (IMBHs) [12–15]. The LVC O1-O2 observations are consistent with the prevention of heavy BH formation by pair-instability supernova (PISN) [11].

For GW190521, the mass of the heavier binary component has a high probability to be within the PISN mass gap [12–15].

BHs of mass $10^2 - 10^5M_{\odot}$, more massive than stellar mass BHs and lighter than supermassive BHs (SMBHs), are traditionally designated IMBHs [16–18]. A conclusive observation of these objects has thus far remained elusive, despite indirect evidence. These include observations of central BHs in galaxies [19, 20], kinematical measurements of massive star clusters [21–23], scaling relations between the mass of the central SMBH and their host galaxies [24], and the mass range of globular clusters [25, 26]. This has led to speculation that IMBHs inhabit the centers of some globular clusters [27–29]. The LVC has also previously searched for binaries of IMBHs explicitly in their GW data, for example [30–32], obtaining null results and establishing an upper limit of 0.2 Gpc $^{-3}$ yr $^{-1}$ on their coalescence rate [33]. The remnant of GW190521 fulfills the above definition of an IMBH.

GW190521 was detected by searches for quasicircular binary coalescences, and there is no evidence in the data for significant departures from such a signal model. However, for any transient with high inferred masses, there are few cycles observable in ground-based detectors, and therefore alternative signal models may also fit the data. This is further addressed in the companion paper [34] that also provides details about physical parameter estimation, and the astrophysical implications of the observation of GWs from this massive system.

Observation.— On May 21, 2019 at 03:02:29 UTC, the LIGO Hanford (LHO), LIGO Livingston (LLO), and Virgo observatories detected a coincident transient signal. A matched-filter search for compact binary mergers, PyCBC Live [35, 36], reported the transient with a network signal-to-noise ratio (SNR) of 14.5 and a false-alarm rate of 1 in 8 yr, triggering the initial alert. A weakly-modeled transient search based on Coherent WaveBurst (cWB) [37] in its IMBH search configuration [30] reported a signal with a network SNR of 15.0 and a false-alarm rate lower than 1 in 28 yr. Two other matched-filter pipelines, SPIIR [38] and GstLAL [39], found con-

sistent candidates albeit with higher false-alarm rates. The identification, localization and classification of the transient as a binary BH merger were reported publicly within ≈ 6 min, with the candidate name S190521g [40, 41].

A second significant GW trigger occurred on the same day at 07:43:59 UTC, S190521r [42]. Despite the short time separation, the inferred sky positions of GW190521 and S190521r are disjoint at high confidence, and so the events are not related by gravitational lensing. Further discussions pertaining to gravitational lensing and GW190521 are presented in the companion paper [34].

GW190521, shown in Figure 1, is a short transient signal with a duration of approximately 0.1 s and around 4 cycles in the frequency band 30–80 Hz. A peak signal frequency of about 60 Hz and the assumption that the source is a compact binary merger imply a massive system.

Data.— The LIGO and Virgo strain data is conditioned prior to its use in search pipelines and parameter estimation analyses. During online calibration of the data [47], narrow spectral features (lines) are subtracted using auxiliary witness sensors. Specifically, we remove from the data the 60 Hz US mains power signature (LIGO), as well as calibration lines (LIGO and Virgo) that are intentionally injected into the detectors to measure the instruments’ responses. During online calibration of Virgo data, broadband noise in the 40–1000 Hz frequency range is subtracted from the data [48]. The noise-subtracted data produced by the online calibration pipelines is used by online search pipelines and initial parameter estimation analyses.

Subsequent to the subtraction conducted within the online calibration pipeline, we perform a secondary offline subtraction [49] on the LIGO data with the goal of removing non-linear sidebands around the US mains power frequency, caused by low frequency modulation of the 60 Hz noise coupling. Since the subtraction of these sidebands is not expected to significantly improve the sensitivity of search algorithms, it is only used in offline parameter estimation of GW190521. Although GW190521 demonstrates a peak frequency of about 60 Hz, there is no evidence that the power mains contribute coherent power to the recovered signal. Voltage monitors and magnetometers installed at each LIGO site show no evidence of significant power fluctuations at the time of the event.

At the time of GW190521, the LHO, LLO and Virgo detectors were observing in their nominal operational O3 state. Low-latency data quality checks [50] did not indicate any transient noise in the vicinity of this event. Four minutes after GW190521, LHO microphones recorded the sound of a nearby helicopter, which also affected the GW strain data. This noise does not impact the confidence of the detection and the affected data is not used for parameter estimation. More thorough analyses per-

formed at higher latency [3, 50] find no evidence that GW190521 is due to, or influenced by, instrumental or environmental noise.

To further confirm that GW190521 is not a noise artifact, we followed the treatment in [3, 50] and investigated potential sources of non-stationary noise typically found in the same frequency band measured for GW190521. The false-alarm rates calculated by the search pipelines estimate the rate of random coincidences of all glitches from the analysis period. Subsequent evaluation of the background noise relevant to an event does not change its calculated false-alarm rate, but serves solely as an event validation procedure. During local daytime hours, the LLO detector exhibits non-stationary noise which is consistent with scattered light due to excess ground motion in the 1–3 Hz band [3]. It produces a variation of the detector noise below 50 Hz, appearing as a periodic sequence of short duration transients. A similar type of noise is also observed in the LHO detector but at significantly lower rate. GW190521 was detected at 03:02:29 UTC, at which time the 1–3 Hz ground motion was low and the GW strain data is not exhibiting the characteristic non-stationarity associated with excessive scattered light. Both detectors also exhibit populations of short duration, band-limited transients (blip glitches) [51, 52], which often demonstrate a characteristic frequency of ~ 50 Hz. These transients are not found in coincidence between the LHO and LLO detectors (except by random occurrence) and GW190521 does not demonstrate the typical frequency-domain power distribution of blip glitches.

Detection significance.— After the identification by the low-latency analyses described above, GW190521 was also identified by offline analyses. These analyze strain data with improved calibration and updated data-quality vetoes, which are not available in low latency, and hence update the low-latency results. The offline analyses use the cWB [37, 53, 54], GstLAL [39, 55–59], and PyCBC [35, 60–65] pipelines. cWB searches for short transient signals with minimal assumptions on their waveform. GstLAL and PyCBC search for coalescences of compact objects using matched filtering with banks of quasicircular, quadrupolar-mode-only, nonprecessing templates [66–72].

We performed the offline cWB analyses (see Supplemental Material) using two detector configurations: one restricted to the LIGO detectors, and one including Virgo as well. These two analyses identified GW190521 with network SNRs of 14.4 and 14.7 respectively, and with event parameters well within the limits defined by the analysis selection cuts. The LIGO-only analysis was used to establish the false-alarm rate for GW190521. The analysis including Virgo produced the waveform reconstruction. The GW190521 false-alarm rate was estimated from the analysis of time-shifted LIGO data. The background is equivalent to 9800 yr of observation and con-

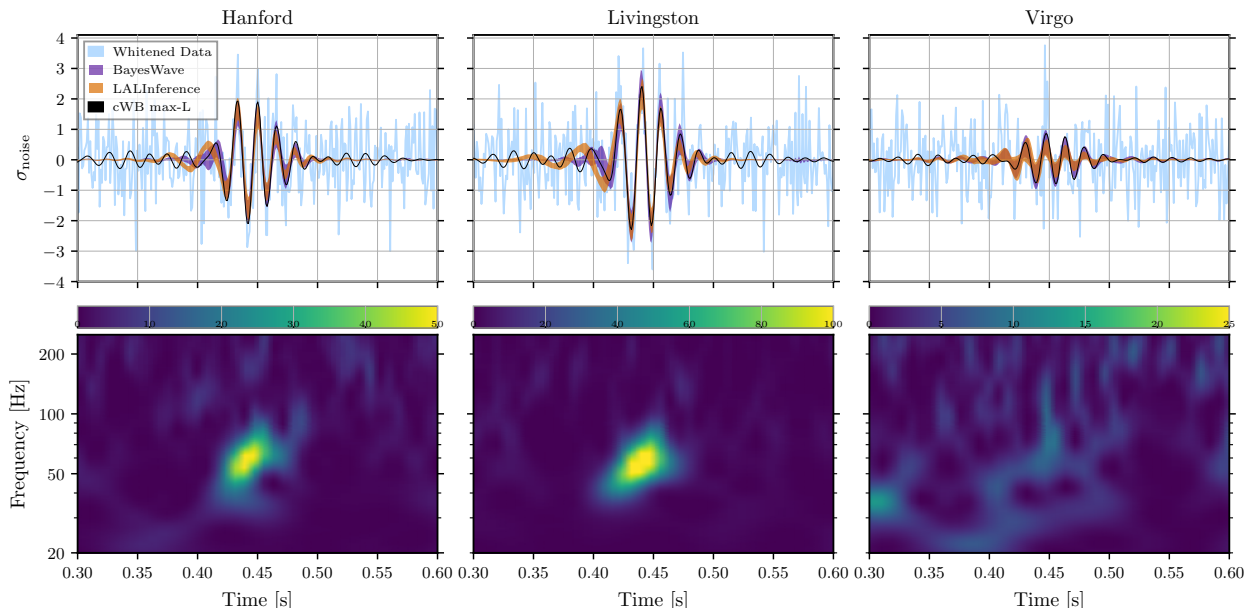


FIG. 1. The GW event GW190521 observed by the LIGO Hanford (left), LIGO Livingston (middle) and Virgo (right) detectors. Times are shown relative to May 21, 2019 at 03:02:29 UTC. The top row displays: the time-domain detector data after whitening by each instrument’s noise amplitude spectral density (light blue lines); the point estimate waveform from the cWB search [37] (black lines); the 90% credible intervals from the posterior probability density functions of the waveform time series, obtained via Bayesian inference (LALInference [43]) with the NRSur7dq4 binary BH waveform model [44] (orange bands), and with a generic wavelet model (BayesWave [45], purple bands). The ordinate axes are in units of noise standard deviations. The bottom row displays the time-frequency representation of the whitened data using the Q transform [46].

tains only two events ranked higher than GW190521, both consistent with random coincidences of short duration (~ 1 cycle) glitches observed in the LIGO frequency band 20–100 Hz. The estimated background results in a false-alarm rate of 1 in 4900 yr for GW190521, which constitutes a confident detection of a GW transient.

The offline analysis conducted by GstLAL (see Supplemental Material) identified GW190521 with a network matched-filter SNR of 14.7 and a false-alarm rate of 1 in 829 yr. The large difference in GstLAL significance reported by its online and offline configurations is due to an improvement in the template bank during O3 that greatly enhanced GstLAL’s sensitivity to mergers of high-mass compact objects.

The offline analysis performed by PyCBC (see Supplemental Material) identified GW190521 with a network matched-filter SNR of 12.6 and a false-alarm rate of 1 in 0.94 yr. The difference between the online and offline SNRs and significances reported by PyCBC is consistent with the fact that the offline analysis does not include Virgo data, with differences in how the two analyses generate and rank their triggers, with minor differences in the placement of the templates, and with the different calibrations of the input strain data. The relatively high false-alarm rate in the offline analysis may be explained by the sparseness of PyCBC’s template bank in the parameter region of GW190521, by the response of the trigger ranking statistic to very high-mass events, or a com-

bination of both effects (see Supplemental Material).

The most massive binary BH merger previously reported by the LVC, GW170719, had the same ordering of significances in cWB, GstLAL and PyCBC as GW190521, and a simulation showed that larger significances in cWB for such heavy BH mergers are not uncommon [3]. Matched-filter searches based on quasicircular nonprecessing templates and cWB have also been compared using broader simulations of heavy BH mergers, including precession and higher-order multipole moments, also concluding that cWB is often more sensitive [73, 74]. We performed a similar simulation campaign for GW190521 in order to further understand the different significances. We simulated thousands of signals compatible with the parameters inferred for the event under the assumption of a quasicircular BH merger, using the NRSur7dq4 waveform model described in the next section, which includes precession and higher-order multipole moments. The simulated sources have merger times distributed uniformly over several days surrounding GW190521, so as to sample many different realizations of the detector noise. The right ascensions have been correspondingly corrected in order to cancel the effect of the Earth rotation, which would lead to different projections of the strain polarizations on the detectors. We added the signals into the data surrounding the event, re-ran the search pipelines with the same configuration used for the offline analysis, and counted the number of

signals recovered by each pipeline. cWB, GstLAL and PyCBC recovered respectively 36%, 45%, and 11% of the simulated signals at a false-alarm rate better than 1 in 4900 yr. The fraction of signals found at a false-alarm rate in cWB better than 1 in 4900 yr and a false-alarm rate in PyCBC worse than 1 in 0.94 yr is 2.7%, which is small but not negligible. The fraction found at a false-alarm rate in cWB better than 1 in 4900 yr and a false-alarm rate in GstLAL worse than 1 in 829 yr is 7.8%. Hence, if GW190521 is a quasicircular binary BH merger, the observed combination of significances in cWB, GstLAL and PyCBC is not particularly surprising.

Astrophysical source.— GW190521 is qualitatively different from previous detections [3, 6, 7] due to the small number of cycles and maximum frequency in the sensitive band of the detectors. Hence, its astrophysical interpretation as a quasicircular compact binary merger warrants more discussion than previous events. Alternative scenarios, such as an eccentric collision [75], become more relevant and are discussed in the companion paper [34]. Nevertheless, the quasicircular BH merger scenario remains the most plausible and we will proceed under this assumption in the rest of this letter.

We performed Bayesian parameter inference on GW190521 using three waveform models for quasicircular binary BHs including the effects of higher order multipole moments and precession. These are the numerical relativity surrogate model NRSur7dq4 [44], the effective-one-body model SEOBNRv4PHM [76, 77] and the phenomenological model IMRPhenomPv3HM [78]. To compute the evidence for higher order modes and precession, we also compared the data with the aforementioned models, omitting these effects. We analysed 8 s of data around the time of GW190521. We impose uniform priors on the redshifted component masses, on the individual spin magnitudes and on the square of the luminosity distance. We impose an isotropic prior on the source and the spin orientations. We produce posterior distributions marginalized over calibration uncertainties. For the NRSur7dq4 and IMRPhenomPHM runs, we made use of the LALInference software package [43] while the SEOBNRv4PHM runs were done using the RIFT algorithm [79]. We find that despite differences in how these waveform models are computed, and the fact that we needed to sample over parameters outside their calibration regions [80], all yield broadly consistent results [34]. In addition, direct comparison of the data to numerical relativity simulations [81–83], using the RIFT algorithm, yields consistent results. In the following we quote results obtained using the NRSur7dq4 model. This choice is motivated by this being the only model that has been calibrated to numerical simulations of precessing BH binaries. In the companion paper, we present results for all three models [34].

Figure 2 shows our estimated 90% credible regions for the individual masses of GW190521. We estimate indi-

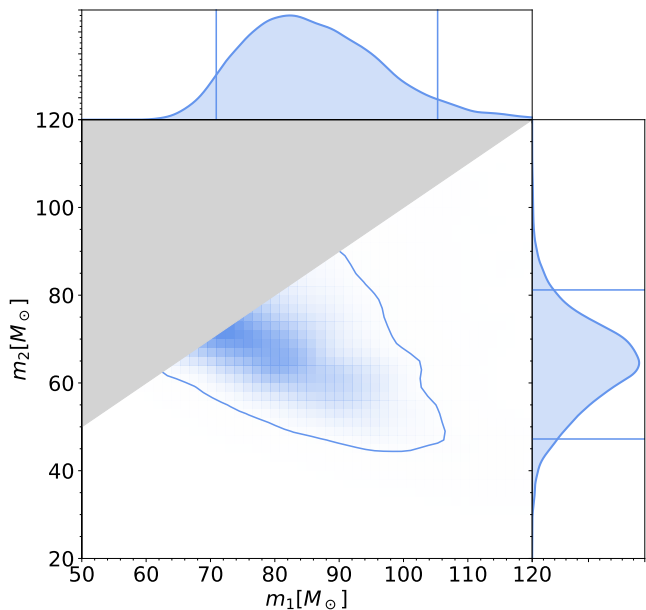


FIG. 2. Posterior distributions for the progenitor masses of GW190521 according to the NRSur7dq4 waveform model. The 90% credible regions are indicated by the solid contour in the joint distribution and by solid vertical and horizontal lines in the marginalized distributions.

vidual components with $(m_1, m_2) = (85^{+20}_{-14}, 65^{+17}_{-17}) M_\odot$ and a total mass $149^{+24}_{-16} M_\odot$. To quantify compatibility with the PISN mass gap, we find the probability of the primary component being below $65 M_\odot$ to be 0.36%. The estimated mass and dimensionless spin magnitude of the remnant object are $M_f = 142^{+23}_{-16} M_\odot$ and $\chi_f = 0.72^{+0.10}_{-0.11}$ respectively. The posterior for M_f shows no support below $100 M_\odot$, making the remnant the first conclusive direct observation of an IMBH.

The left panel of Figure 3 shows the posterior distributions for the magnitude and tilt angle of the individual spins, measured at a reference frequency of 11 Hz. First, we obtain posteriors peaking close to the $\chi = 1$ limit imposed by cosmic censorship [84]. Second, the data shows evidence for large tilt angles, indicating that the spins are unaligned with the orbital angular momentum. This leads to a strong spin-orbit coupling that causes the orbital plane to precess [85, 86]. The impact of precession in the signal is commonly parametrised by the effective precession spin parameter χ_p [87, 88] while the effective inspiral spin parameter χ_{eff} parametrises the impact of the spin components aligned with the orbital angular momentum [89–92]. Figure 3 shows the corresponding posterior distributions. We estimate $\chi_{\text{eff}} = 0.07^{+0.30}_{-0.35}$ and $\chi_p = 0.63^{+0.28}_{-0.38}$. While the posterior for χ_{eff} is close to the prior, the posterior for χ_p differs from it, indicating that precession may be playing a non-negligible role. We evaluated the Bayesian evidence for a precessing orbital plane by performing model selection with models omit-

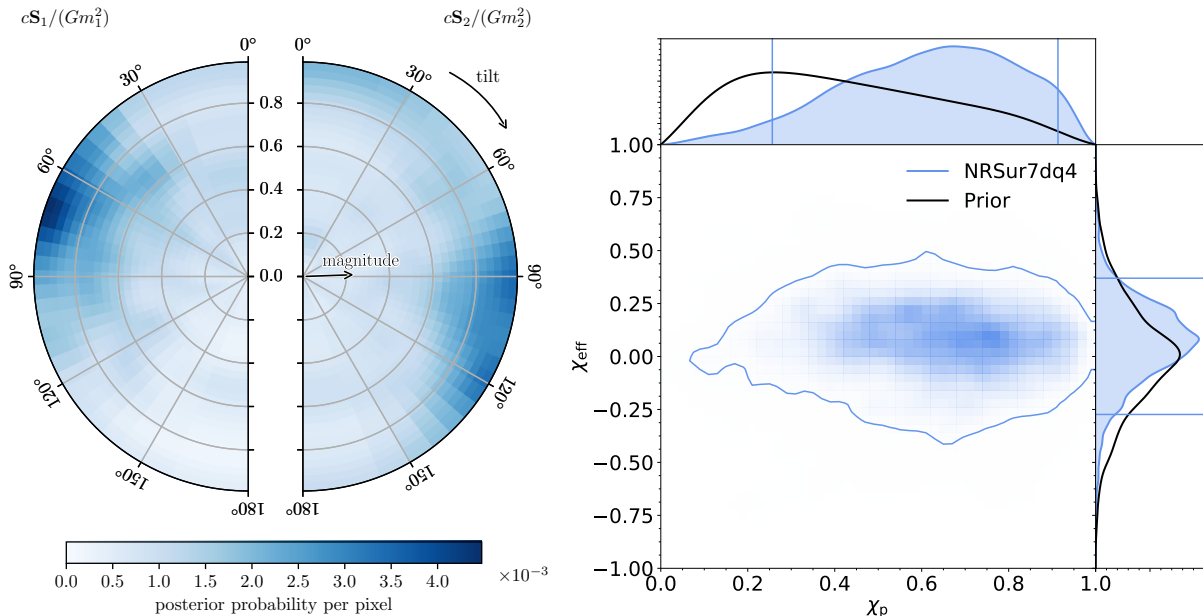


FIG. 3. Left: posterior distribution for the individual spins of GW190521 according to the NRSur7dq4 waveform model. The radial coordinate in the plot denotes the dimensionless spin magnitude, while the angle denotes the spin tilt, defined as the angle between the spin and the total angular momentum of the binary. A tilt of 0 indicates that the spin is aligned with the total angular momentum. A nonzero magnitude and a tilt away from 0 and 180 deg imply a precessing orbital plane. Right: posterior distributions for the effective spin and effective in-plane spin parameters. The 90% credible regions are indicated by the solid contour in the joint distribution, and by solid vertical and horizontal lines in the marginalized distributions. The large density for tilts close to 90 deg leads to large values for χ_p and low values for χ_{eff} .

ting and including precession, obtaining a \log_{10} Bayes factor of $0.65^{+0.06}_{-0.06}$ in favour of precession. This indicates a weak preference for a precessing orbital plane.

We estimate the luminosity distance of GW190521 to be $5.3^{+2.2}_{-2.2}$ Gpc, corresponding to a redshift of $0.82^{+0.27}_{-0.29}$, assuming a Λ CDM cosmology with Hubble parameter $H_0 = 67.9 \text{ km s}^{-1} \text{ Mpc}^{-1}$ [93]. Figure 4 shows the joint posterior distribution for the luminosity distance and the inclination angle between the total angular momentum of the binary and the line-of-sight, θ_{JN} . We constrain $\sin(\theta_{JN}) < 0.74$ at the 90% credible level. Signals emitted at such inclinations are dominated by the quadrupolar (2, 2) mode [94–97]. Indeed, we obtain a \log_{10} Bayes Factor of $-0.36^{+0.06}_{-0.06}$ disfavouring the presence of higher order multipole moments in the data. Despite this fact, as described in [98], models that include higher modes still lead to more precise estimates of the distance and inclination of the source. The reason is that higher modes are more prominent in signals with large inclination angles, especially when the signal is dominated by the merger and ringdown portions, thereby allowing us to discard those angles [96, 97, 99, 100].

The large individual and total masses of GW190521, and the low likelihood that the primary originated from a stellar collapse given theoretical constraints on supernova physics, strongly suggest a different formation channel from BH binaries previously reported. We discuss

various possible channels in detail in [34] including hierarchical merger, stellar merger and formation in an active galactic nucleus environment. With only one such system so far confirmed, uncertainties on the formation channel and corresponding merger rate are necessarily very large. Under the simplifying assumption that the component masses and spins GW190521 are representative of a population of merging binaries, we estimate a merger rate $0.13^{+0.30}_{-0.11} \text{ Gpc}^{-3} \text{ yr}^{-1}$ [34], consistent with the prior upper bounds set in [33].

Waveform reconstruction.— GW190521 waveform reconstructions are obtained through a templated LALInference analysis [43], and two signal-agnostic analyses, cWB [37, 101] and BayesWave [45, 102]. Both signal-agnostic analyses reconstruct signal waveforms as a linear combination of wavelets: cWB obtains point estimate waveforms with the constrained maximum likelihood method while BayesWave reconstructs waveforms by drawing posterior samples from an unmodeled Bayesian analysis. Figure 1 shows broad agreement between the waveform reconstructions.

For a quantitative comparison of the cWB point estimate waveform w and the template h , we calculate the overlap, or match $(w|h)/\sqrt{(w|w)(h|h)}$, where $(w|h)$ denotes the noise-weighted network inner product [103]. We randomly draw signals from the templated inference analysis, inject these into data surrounding GW190521,

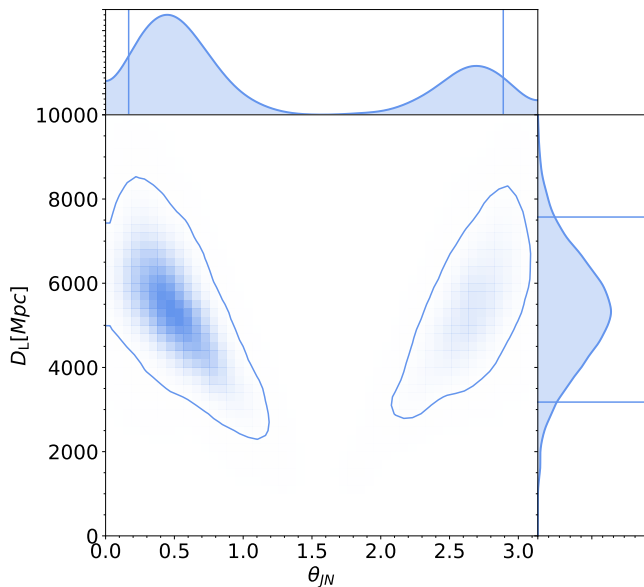


FIG. 4. Posterior distributions for the luminosity distance and the inclination angle of GW190521, according to the NR-Sur7dq4 waveform model. The inclination angle indicates the angle between the line-of-sight and the total angular momentum of the binary. For non-precessing binaries, this is equal to the angle between the orbital angular momentum and the line-of-sight. We find the total angular momentum is likely to be closer to the line-of-sight than to the orthogonal direction. The solid lines and the central contour denote 90% credible regions.

Parameter	
Primary mass	$85^{+20}_{-14} M_{\odot}$
Secondary mass	$65^{+17}_{-17} M_{\odot}$
Primary spin magnitude	$0.64^{+0.32}_{-0.55}$
Secondary spin magnitude	$0.68^{+0.29}_{-0.59}$
Total mass	$149^{+24}_{-16} M_{\odot}$
Mass ratio ($m_2/m_1 \leq 1$)	$0.78^{+0.20}_{-0.31}$
Effective inspiral spin parameter (χ_{eff})	$0.07^{+0.30}_{-0.35}$
Effective precession spin parameter (χ_p)	$0.63^{+0.28}_{-0.38}$
Luminosity Distance	$5.3^{+2.2}_{-2.2}$ Gpc
Redshift	$0.82^{+0.27}_{-0.29}$
Final mass	$142^{+23}_{-16} M_{\odot}$
Final spin	$0.72^{+0.10}_{-0.11}$
$P(m_1 < 65 M_{\odot})$	0.36%
\log_{10} Bayes factor for precessing plane	$0.65^{+0.06}_{-0.06}$
\log_{10} Bayes factor for higher harmonics	$-0.36^{+0.06}_{-0.06}$

TABLE I. Parameters of GW190521 according to the NR-Sur7dq4 waveform model. We quote median values with 90% credible intervals that include statistical errors.

and reconstruct the injections with cWB. The overlaps between the simulated signals and the corresponding cWB reconstructions define the null distribution, which takes into account the waveform reconstruction errors and fluctuations of the detector noise. The median and 90% confidence interval for the null distribution are $0.93^{+0.03}_{-0.05}$. The overlap between the cWB point estimate for GW190521 and the maximum-likelihood NRSur7dq4 template is 0.89 and is consistent with the null distribution.

Similarly, the overlap [102] between the median BayesWave waveform and the maximum likelihood NR-Sur7dq4 template is 0.89. A signal residual test is performed by subtracting the maximum likelihood NR-Sur7dq4 template from the data and then searching for a residual signal using BayesWave [104]. The residual search result is compared to the distribution found from the analysis of the off-source data surrounding the event. This comparison results in a p-value of 0.26, indicating that the residual is fully consistent with noise.

Black hole ringdown.— We analyzed the ringdown portion of GW190521 using a damped sinusoid to fit the least-damped ringdown mode [105, 106]. Starting 12.7 ms after the peak of the complex strain (corresponding to $\sim t_{\text{peak}} + 10 G(1+z)M_f/c^3$ in units of the redshifted remnant mass $(1+z)M_f$ [107], using median values from the NRSur7dq4 approximant), the analysis estimates a frequency $f = 66^{+4}_{-3}$ Hz and damping time $\tau = 19^{+9}_{-7}$ ms, with a Bayes factor between signal and noise of $\log_{10}(B_{s/n}) = 25.45 \pm 0.02$. By imposing predictions of perturbation theory on the frequency of the GW emission [108] we infer the final redshifted mass and dimensionless spin to be $(1+z)M_f = 252^{+63}_{-64} M_{\odot}$ and $\chi_f = 0.65^{+0.22}_{-0.48}$ (see Fig. 5). All quoted values correspond to median and 90% credible intervals. Accounting for redshift, these results are consistent with the full-waveform analysis when using NR fits to predict the remnant quantities [44, 108–112]. Additional detailed investigations are reported in the companion paper [34].

Summary.— GW190521 is a short duration signal consistent with a binary BH merger. According to state of the art models for quasicircular binaries, the progenitor BHs show mild evidence for high spins and a precessing orbit, and the heavier component mass $85^{+20}_{-14} M_{\odot}$ sits in the PISN mass gap. The merger left behind a remnant with a final mass of $142^{+23}_{-16} M_{\odot}$, making this a direct observation of the formation of an IMBH. The remnant ringdown signal is compatible with the full waveform analysis and general relativity. Further details on the properties of GW190521 are discussed in the companion paper, together with its astrophysical implications [34]. The short duration of GW190521 also invites other interpretations for the source [34]. As the low frequency sensitivity improves for Advanced LIGO and Advanced Virgo [113] further massive binary BH events should be observed. Third generation ground based GW detec-

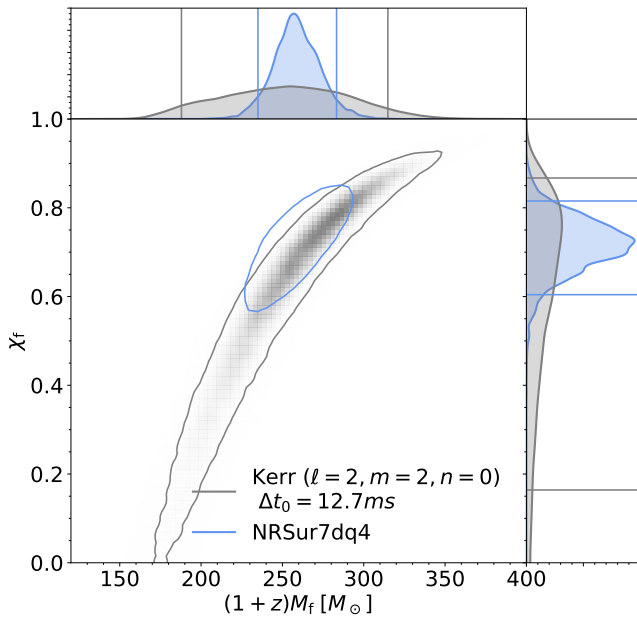


FIG. 5. Redshifted remnant mass and spin inferred from the least-damped $\ell = m = 2$ ringdown mode. The analysis was carried out 12.7 ms ($\sim 10 G(1+z)M_f/c^3$) after the reference time $t_{\text{peak}}^{\text{H}} = 1242442967.4306$ for the Hanford detector (appropriately time-shifted in the other detectors assuming the maximum likelihood value on the sky position inferred from the NRSur7dq4 approximant). The blue contour represents the 90% credible region of the prediction from the full-waveform analysis.

tors [114–116] and LISA [117] will be important instruments to study these systems.

Acknowledgments.— The authors gratefully acknowledge the support of the United States National Science Foundation (NSF) for the construction and operation of the LIGO Laboratory and Advanced LIGO as well as the Science and Technology Facilities Council (STFC) of the United Kingdom, the Max-Planck-Society (MPS), and the State of Niedersachsen/Germany for support of the construction of Advanced LIGO and construction and operation of the GEO600 detector. Additional support for Advanced LIGO was provided by the Australian Research Council. The authors gratefully acknowledge the Italian Istituto Nazionale di Fisica Nucleare (INFN), the French Centre National de la Recherche Scientifique (CNRS) and the Netherlands Organization for Scientific Research, for the construction and operation of the Virgo detector and the creation and support of the EGO consortium. The authors also gratefully acknowledge research support from these agencies as well as by the Council of Scientific and Industrial Research of India, the Department of Science and Technology, India, the Science & Engineering Research Board (SERB), India, the Ministry of Human Resource Development, India, the Spanish Agencia Estatal de Invest-

tigación, the Vicepresidència i Conselleria d’Innovació, Recerca i Turisme and the Conselleria d’Educació i Universitat del Govern de les Illes Balears, the Conselleria d’Innovació, Universitats, Ciència i Societat Digital de la Generalitat Valenciana and the CERCA Programme Generalitat de Catalunya, Spain, the National Science Centre of Poland, the Swiss National Science Foundation (SNSF), the Russian Foundation for Basic Research, the Russian Science Foundation, the European Commission, the European Regional Development Funds (ERDF), the Royal Society, the Scottish Funding Council, the Scottish Universities Physics Alliance, the Hungarian Scientific Research Fund (OTKA), the French Lyon Institute of Origins (LIO), the Belgian Fonds de la Recherche Scientifique (FRS-FNRS), Actions de Recherche Concertées (ARC) and Fonds Wetenschappelijk Onderzoek – Vlaanderen (FWO), Belgium, the Paris Île-de-France Region, the National Research, Development and Innovation Office Hungary (NKFIH), the National Research Foundation of Korea, Industry Canada and the Province of Ontario through the Ministry of Economic Development and Innovation, the Natural Science and Engineering Research Council Canada, the Canadian Institute for Advanced Research, the Brazilian Ministry of Science, Technology, Innovations, and Communications, the International Center for Theoretical Physics South American Institute for Fundamental Research (ICTP-SAIFR), the Research Grants Council of Hong Kong, the National Natural Science Foundation of China (NSFC), the Leverhulme Trust, the Research Corporation, the Ministry of Science and Technology (MOST), Taiwan and the Kavli Foundation. The authors gratefully acknowledge the support of the NSF, STFC, INFN and CNRS for provision of computational resources. We would like to thank all of the essential workers who put their health at risk during the COVID-19 pandemic, without whom we would not have been able to complete this work. This document has been assigned the LIGO document number LIGO-P2000020.

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